

Alternate Method of Estimating Nigerian Hydrocarbon Reserves.

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ABSTRACT

Reserves estimation of most oil fields is often performed through the Material Balance and Volumetric methods. Alternatively, a simple Estimation Model and Least Squares Regression may be useful or appropriate. This model used alongside with Linear Regression Analysis in this study gives improved estimates of the fields considered, hence can, be used in other Nigerian Fields with recent production history.

(Keywords: Nigerian hydrocarbon reserves, petroleum production, estimation model, linear least squares regression method, completed wells)

INTRODUCTION

The process of estimating oil and gas reserves for a producing field continues throughout the life of the field. There is always uncertainty in making such estimates. The level of uncertainty is affected by the following factors: reservoir type, source of reservoir energy, quantity and quality of the geological, engineering, and geophysical data, assumptions adopted when making the estimate, available technology, and experience and knowledge of the evaluator [1]. The magnitude of uncertainty, however, decreases with time until the economic limit is reached and the ultimate recovery is realized [1].

Petroleum (or any other natural resource) reserves cannot be measured directly. They are estimates of future production under certain conditions which may or may not be well specified, but which include economic assumptions, knowledge of the feasibility of projects to extract the resources, and geological information. Judgment is involved and different estimates for the same field are legitimately possible [2].

Statistical estimation of oil and gas reserves is the estimation of petroleum reserves using historical records of production, exploratory drilling, pressure history and other factors that influence reserves [3]. Reserve estimation is useful in evaluation of exploration and development expenditures, to determine the market value of a field in connection with possible purchase or sale. It is also used to determine the feasibility of secondary recovery projects and other special recovery projects.

Reserves can be divided into primary and secondary reserves. Primary reserves are the estimated future commercial production recoverable by normal or primary method as a result of energy availability in the reservoir while secondary reserves are the estimated future commercial production which will be recovered in addition to the primary reserves as a result of pressure maintenance, water flooding or other secondary methods [4].

Unproved reserves are less certain to be recovered than proved reserves and may be sub-classified as probable or possible to denote increasing uncertainty. Proved reserves can be estimated with reasonable certainty to be recoverable under current economic conditions which include prices and costs prevailing at the time of the estimate [5]. Proved reserves may be developed or under developed. It must have facilities to process and transport those reserves to markets that are operational at the time of the estimate or there is commitment or reasonable expectation to install such facilities in the future [5].

The additional reserve each year is dependent on reserves found by exploratory drilling in new pools, in new fields and reserves done to re-

evaluate the basic geological and engineering data of existing fields. A discovery during one year will result in the drilling of additional wells during subsequent production and these wells add productive acreage to the previously estimated proved area [6].

Other reserves estimation methods includes: Analogy, Volumetric, Decline analysis, Material balance, and Reservoir simulation [7]. Most of the field data required are not obtainable until the reservoir has produced for substantial period, therefore evaluated reserve of new field using other reserves estimation methods are not reliable.

AIMS OF THE STUDY

The aims of this study are to measure the crude oil potential of Nigerian fields and to select the best statistical method for evaluating the hydrocarbon reserves in Nigeria. A mathematical model for petroleum reserves estimate based on extrapolation of exploratory drilling trend was developed. Additional reserve factor due to revision of existing field is included in the model. The method of Least Square Regression is employed to solve the constants in the developed model and to compare the estimated reserves from the actual reserves.

GEOLOGICAL SETTINGS OF THE NIGER DELTA REGION OF NIGERIA

Niger Delta is a large arcuate Tertiary prograding sedimentary complex deposited under transitional marine, deltaic, and continental environments since Eocene in the North to Pliocene in the South. Located within the Cenozoic formation of Southern Nigeria in West Africa, it covers an area of about 75,000 Km [8] from the Calabar Flank and Abakaliki Trough in Eastern Nigeria to the Benin Flank in the West, and it opens to the Atlantic ocean in the South where it protrudes into the Gulf of Guinea as an extension from the Benue Trough and Anambra Basin provinces [9].

The Niger Delta as a prograding sedimentary complex is characterized by a coarsening upward regressive sequences. The overall regressive sequence of clastic sediments was deposited in a series of offlap cycles that were interrupted by periods of sea level change [10]. These periods

resulted in episodes of erosion or marine transgression.

Stratigraphically, the Tertiary Niger Delta is divided into three Formations, namely Akata Formation, Agbada Formation, and Benin Formation [11]. The Akata Formation at the base of the delta is predominantly under-compacted, over-pressured sequence of thick marine shales, clays and siltstones (potential source rock) with turbidite sandstones (potential reservoirs in deep water). It is estimated that the formation is up to 7,000 meters thick [12]. The Agbada Formation, the major petroleum-bearing unit about 3700m thick, is alternation sequence of paralic sandstones, clays and siltstone and it is reported to show a two-fold division [13]. The upper Benin Formation overlying Agbada Formation consists of massive, unconsolidated continental sandstones.

WHY “LINEAR REGRESSION ANALYSIS (LRA)” FOR HYDROCARBON RESERVES?

The “Method of Least Squares” that is used to estimate parameters estimates was independently developed in the late 1700’s and the early 1800’s by the mathematician Karl Friedrich Gauss, Adrien Marie Legendre, and Robert Adrain [14], [15], [16] working in Germany, France, and America, respectively. In the least squares method the unknown parameters are estimated by minimizing the sum of the squared derivatives between the data and the model. The minimization process reduces the over-determined system of equations formed by the data to a sensible system of p (where p is the number of parameters in the functional part of the model) equations in p unknowns. This new system of equations is then solved to obtain the parameter estimates [16].

Linear Regression Analysis (LRA) is by far the most widely used modeling method adapted to a broad range of situations that are outside its direct scope. It plays a strong underlying role in many other modeling methods like Non Linear Least Squares Regression Method, Weighted Least Squares Regression, and LOESS [14]. Linear Regression Analysis (LRA) can be used directly with an appropriate data set to fit complex data. It has earned its place as the primary tool for process modeling because of its effectiveness and completeness.

Though there are types of data that are better described by functions that are non-linear in the parameters, many process in science and engineering are well described by linear models. This is because either the processes are inherently linear or because, over short range, any process can be well-approximated by a linear model. The estimates of the unknown parameters obtained from linear regression are the optimal estimates from a broad class of possible parameter estimates under the usual assumptions used for process modeling. Practically speaking, Linear Regression Analysis (LRA) makes very efficient use of the data. Good results can be obtained with relatively small data sets [17].

ESTIMATION MODEL DEVELOPMENT

Model's Theory

The model is based on the principle that the reserve at the end of any year will be the sum of the reserve at the beginning of that year and additional reserve minus productions during that year. Additional reserves of hydrocarbons in any year are broken down into two established categories: Those attributable to recoveries as a result of exploratory effort in new pools in new fields. Reserves attributed to revisions as a result of re-evaluation on the existing fields.

Newly discovered petroleum reservoirs, even in existing fields are always fully developed during the year of recovery [18]. Therefore, the year and reserve estimates of discoveries generally represent only a part of the reserves that will ultimately be assigned to these new reservoirs. A discovery during one year will usually result in the drilling of additional wells during subsequent years and generally these new wells will increase the previously estimated productive area [19].

Additional producing wells in a reservoir not only add to the estimated productive area but also help to improve the basic geologic and engineering data. Early estimates of porosity, interstitial water, pay thickness and other important reservoir factors may be reviewed therefore from future wells. As field development continues, production history accumulates and the most accurate methods of pressure maintenance and secondary recovery factor are formulated [20].

Estimation Model Derivation

Reserve at the end of any year is defined as:

$$R_x = R(x-1) + R_x^+ - Q_x + A_x \quad (1)$$

Where,

X is the number of terms in years

R_x is the estimated reserve at the end of xth year.
 $R(x-1)$ is the estimated reserve at the end of (x-1)th year.

R_x^+ is the additional reserve during the xth year due to exploratory drilling.

Q_x is the production in the xth year

A_x is the additional reserve in the xth year due to revision of existing fields.

Additional reserve due to exploratory drilling R_x^+ based on historical trend is defined as:

$$R_x^+ = (m + nP_x) - C_{x-1} \quad (2)$$

Where,

m is the intercept of regression line of plot of cumulative additional reserve against cumulative number of completed wells.

n is the rate of change of cumulative additional reserve with cumulative number of completed wells.

P_x is the cumulative number of completed wells at the end of xth year.

C_{x-1} is the cumulative additional reserve at the end of (x-1)th year.

In general, $(m + nP_x)$ represents cumulative additional reserve due to exploratory effort in the xth year. Thus, it can be represented by C_x :

$$C_x = m + nP_x \quad (3)$$

Where,

C_x is the cumulative additional reserve in the xth year. The Estimation Model can therefore be approximated as:

$$R_x = R(x-1) + C_x - C_{x-1} - Q_x + A_x \quad (4)$$

$$= R(x-1) + (m + nP_x) - C_{x-1} - Q_x + A_x \quad (5)$$

$$= R(x-1) + (m + nP_x) + A_x - (C_{x-1} + Q_x) \quad (6)$$

Constants m and n can be calculated by Linear Regression Analysis (LRA). Equation (6) represents the general form of the Estimation Model.

Linear Regression Analysis (LRA)

The concept of linear regression is concerned with an investigation of the dependence of one variable on a linear combination of independent variable. When the dependent variable is expressed linearly in terms of one independent variable, the linear expression is said to be simple while it is said to be multiple when the dependent variables is expressed linearly in terms of several independent variables. In this study, the linear regression is simple since only one independent variable is involved.

From Equation (3):

$$C_x = m + nP_x$$

C_x from this equation is the calculated C_x which may not correspond to the observed C_x .

Let $C_x' =$ observed C_x .

Then the error term, T_x is calculated as:

$$T_x = C_x - C_x' \quad (7)$$

$$T_x = (nP_x + m) \quad (8)$$

To minimize the error, a relation of the form is introduced:

$$S = \sum T_x^2 \quad (9)$$

Using least squares to minimize S, so that:

$$\frac{ds}{dT} = 0; \frac{ds}{dm} = 0$$

$$\frac{ds}{dn} = 2 \sum t \frac{dT_x}{x dn} = 0$$

$$= 2 \sum (nP_x + m - C_x) P_x = 0$$

$$= n \sum P_x^2 + m \sum P_x - \sum C_x P_x = 0$$

Therefore,

$$\sum C_x P_x = m \sum P_x + n \sum P_x^2 \quad (10)$$

Similarly,

$$\frac{ds}{dm} = 2 \sum T_x \frac{dT_x}{x dm} = 0$$

$$= 2 \sum (nP_x + m - C_x) \times 1 = 0$$

$$= n \sum P_x + m - \sum C_x = 0$$

$$= n \sum P_x + km - \sum C_x = 0$$

Therefore,

$$\sum C_x = km + n \sum P_x \quad (11)$$

Where,

k is the number of data used in trend analysis.

Equations (10) and (11) can then be solved simultaneously to obtain m and n.

$$\sum C_x = km + n \sum P_x$$

$$\sum C_x P_x = m \sum P_x + n \sum P_x^2$$

Or

$$\sum P_x C_x = m k \sum P_x + n (\sum P_x)^2 \quad (12)$$

$$k \sum C_x P_x = m k \sum P_x + n \sum P_x^2 \quad (13)$$

$$k \sum C_x - (\sum P_x) (\sum C_x) = (k \sum P_x^2 - (\sum P_x)^2)$$

$$n = \frac{k \sum C_x P_x - \sum P_x C_x}{(k \sum P_x^2 - (\sum P_x)^2)} \quad (14)$$

Substitute Equation (14) in Equation (11):

$$\sum C_x = km + \frac{k \sum P_x \sum C_x P_x - (\sum P_x)^2 \sum C_x}{(k \sum P_x^2 - (\sum P_x)^2)}$$

$$m = \frac{\sum C_x}{k} - \frac{1}{k} \frac{k \sum P_x \sum C_x P_x - (\sum P_x)^2 \sum C_x}{(k \sum P_x^2 - (\sum P_x)^2)} \quad (15)$$

$C_x = m + nP_x$ represents equation of regression line on C_x and P_x .

Estimating Nigerian Total Hydrocarbon Reserves

The developed estimation model can also be used to evaluate the total petroleum reserves in Nigeria.

Recall that:

$$R_x = R(x-1) + (m + nP_x) + A_x - (C_{x-1} + Q_x) \quad (6)$$

Assuming $A_x = 0$, that is no revision of the existing fields used in the reserve estimation, the estimation model will reduce to:

$$R_x = R(x-1) + (m + nP_x) + (C_{x-1} + Q_x) \quad (16)$$

Concept of Correlation and Standard Error of Estimate

Correlation is the degree of relationship between variables, in this case, the cumulated additional reserves and cumulated number of completed wells. The coefficient of correlation can be determined using the Pearson's Product-Moment Method.

$$R = k \frac{k \sum P_x C_x - (\sum P_x) \sum C_x}{\sqrt{(k \sum P_x^2 - (\sum P_x)^2) (k \sum C_x^2 - (\sum C_x)^2)}} \quad (17)$$

Standard error of estimate S is a measure of the scatter about the regression line and is supplied by the quantity.

$$S = \sqrt{\frac{\sum C_x^2 - m(\sum C_x) - n \sum C_x P_x}{k}} \quad (18)$$

ANALYSIS OF RESULTS

The general form of the estimation model is given by:

$$R_x = R(x-1) + C_x - C_{x-1} - Q_x + A_x$$

Where,

R_x = Estimated reserve at the end of xth year.

$R(x-1)$ = Estimated reserve at the end of (x-1)th year.

C_x = Cumulative additional reserve during the xth year due to exploratory drilling at the end of xth year.

C_{x-1} = Cumulative additional reserve at the end of (x-1)th year.

Q_x = Production during the year.

A_x = Additional reserve in the xth year due to revision of existing fields.

$$C_x = (m + nP_x)$$

Where,

P_x is the intercept of regression line of plot of cumulative additional reserve against cumulative number of completed wells.

m and n are constant determined from linear regression model.

Estimation of Fields X and Y Reserves in Nigeria

Two fields considered in Nigeria were assigned X and Y fields due to the sensitive nature of the data [21]. The estimation model is:

$$R_x = R(x-1) + (m + nP_x) + A_x - (C_{x-1} + Q_x).$$

A_x was assumed to be zero, i.e. no revision of the existing fields used in the reserve estimation.

The above equation reduces to:

$$R_x = R(x-1) + (m + nP_x) - (C_{x-1} + Q_x). \quad (16)$$

Coefficient of Correlation

The correlation between the cumulative additional reserve and cumulative number of completed wells can be estimated from Equation 16 using the data shown in Tables 2 and 3.

Table 1: Coefficient of Correlation for Field X and Y (2014).

| Field | Coefficient of Correlation, r |
|-------|-------------------------------|
| X | 0.999817 |
| Y | 0.993728 |

Table 2: Production History of Field X (2014).

| Year | Annual Production (mmbbls) | Reserves (mmbbls) | Additional Reserve (mmbbls) | Cumulative Additional Reserve (mmbbls) | Cumulative No. of Completed Wells |
|------|----------------------------|-------------------|-----------------------------|--|-----------------------------------|
| 1978 | 0.0301 | 0.615 | 0.0348 | 0.3048 | |
| 1979 | 0.0304 | 0.594 | 0.0098 | 0.0446 | 24 |
| 1980 | 0.0363 | 0.560 | 0.0022 | 0.0468 | 24 |
| 1981 | 0.0217 | 0.597 | 0.0587 | 0.1055 | 55 |
| 1982 | 0.0318 | 0.571 | 0.0053 | 0.1108 | 58 |
| 1983 | 0.0258 | 0.554 | 0.0090 | 0.1198 | 62 |
| 1984 | 0.0286 | 0.529 | 0.0041 | 0.1239 | 64 |

Table 3: Production History of Field Y (2014).

| Year | Annual Production (mmbbls) | Reserve (mm bbls) | Additional reserves (mmbbls) | Cumulative additional reserve (mmbbls) | Cumulative No. of completed wells |
|------|----------------------------|-------------------|------------------------------|--|-----------------------------------|
| 1978 | 0.0150 | 0.116 | 0.0201 | 0.0201 | 1.0 |
| 1979 | 0.0153 | 0.142 | 0.0413 | 0.0614 | 31 |
| 1980 | 0.0133 | 0.144 | 0.0148 | 0.0762 | 38 |
| 1981 | 0.0088 | 0.138 | 0.0026 | 0.0788 | 41 |
| 1982 | 0.0057 | 0.133 | 0.0009 | 0.0797 | 42 |
| 1983 | 0.0064 | 0.128 | 0.0012 | 0.0809 | 44 |
| 1984 | 0.0054 | 0.123 | 0.0008 | 0.0817 | 45 |

Table 4: Determination of Constants n and m from Table 2 and 3 using Equation (14) and (15), respectively.

| Field | n | m |
|-------|----------------------|-----------------------|
| X | 0.1949×10^7 | -0.1440×10^7 |
| Y | 0.1807×10^7 | 0.3607×10^7 |

Table 5: Annual Estimated Reserves and Actual Reserves for Field X (2014).

| Year | Estimated Reserve (mmbbls) | Actual Reserves (mmbbls) | Difference |
|------|----------------------------|--------------------------|------------|
| 1979 | 0.596092 | 0.59420 | 0.001892 |
| 1980 | 0.561740 | 0.56010 | 0.001640 |
| 1981 | 0.598499 | 0.59710 | 0.001399 |
| 1982 | 0.527544 | 0.57060 | 0.000739 |
| 1983 | 0.554539 | 0.55380 | 0.000739 |
| 1984 | 0.529836 | 0.52930 | 0.000536 |

Table 6: Annual Estimated Reserve and Actual Reserve for Field Y (2014).

| Year | Estimated Reserve (mmbbls) | Actual Reserves (mmbbls) | Difference |
|------|----------------------------|--------------------------|------------|
| 1979 | 0.138946 | 0.142300 | 0.003354 |
| 1980 | 0.138295 | 0.143300 | 0.005505 |
| 1981 | 0.134915 | 0.137600 | 0.002684 |
| 1982 | 0.131022 | 0.132800 | 0.001778 |
| 1983 | 0.128236 | 0.127600 | 0.000636 |
| 1984 | 0.124643 | 0.123000 | 0.001643 |

The result from Table 1 shows that there is a perfect correlation between cumulative additional reserve and cumulative number of completed wells in the positive direction for both fields.

Applying the constants generated from Equation (14) and (15), respectively, to the developed estimation model of Equation (6) for Field X and Y gives the results in Tables 5 and 6, respectively.

Concept of Correlation Coefficient and Standard Error of Estimate

The correlation between the cumulative additional reserve and cumulative number of completed wells as well as standard error of estimate were evaluated from Equation (17) and (18) respectively using the data in Table 7.

The obtained results of $r = 0.9996208$ and $S = 0.6980 \times 10^6$ for Field X, and $S = 0.2323 \times 10^7$ for Field Y shows that there is perfect correlation

between cumulative additional reserve and cumulative number of completed wells in the positive direction.

Determination of Constants n and m for Nigerian Hydrocarbon Reserves

Applying data in Table 5 to constants n and m expressions gives:

$$n = 0.7527 \times 10^7 \text{ bbls/well and } m = 0.3128 \times 10^9 \text{ bbls/well}$$

The general equation of estimated model therefore becomes:

$$R_x = R(x-1) + (0.3128 \times 10^9 + 0.7527 \times 10^7 P_x) - (C_{x-1} + Q_x). \tag{19}$$

The result obtained from Equation (19) using data in Table 7 is shown in Table 8.

Table 7: Production History of a Named Nigerian Field (2014).

| Year | Annual Production (mmbbls) | Reserve (mmbbls) | Additional reserve (mmbbls) | Cumulative additional reserve (mmbbls) | Cumulative no. of completed wells (mmbbls) |
|------|----------------------------|------------------|-----------------------------|--|--|
| 1970 | 0.3958 | 10.400 | 0.4458 | 0.4958 | 105 |
| 1971 | 0.5596 | 11.200 | 1.3596 | 1.8554 | 223 |
| 1972 | 0.6666 | 12.100 | 1.5666 | 3.420 | 368 |
| 1973 | 0.7484 | 12.700 | 1.3484 | 4.7704 | 520 |
| 1974 | 0.8231 | 12.800 | 0.9231 | 5.6935 | 652 |
| 1975 | 0.6514 | 13.000 | 0.8514 | 6.5449 | 819 |
| 1976 | 0.7568 | 12.800 | 0.5568 | 7.1017 | 936 |
| 1977 | 0.7646 | 12.600 | 0.5648 | 7.6665 | 1033 |

Table 8: Annual Estimated Reserves and Actual Reserves for Nigeria (2014).

| Year | Estimate Reserves (mmbbls) | Actual Reserves (mmbbls) | Variation |
|------|----------------------------|--------------------------|-----------|
| 1971 | 10.728625 | 11.20000 | 0.471375 |
| 1972 | 11.153489 | 12.10000 | 0.946511 |
| 1973 | 11.549245 | 12.70000 | 1.150755 |
| 1974 | 11.719751 | 12.80000 | 1.080249 |
| 1975 | 12.325417 | 13.00000 | 0.674583 |
| 1976 | 12.449317 | 12.80000 | 0.350683 |
| 1977 | 12.414868 | 12.60000 | 0.185132 |

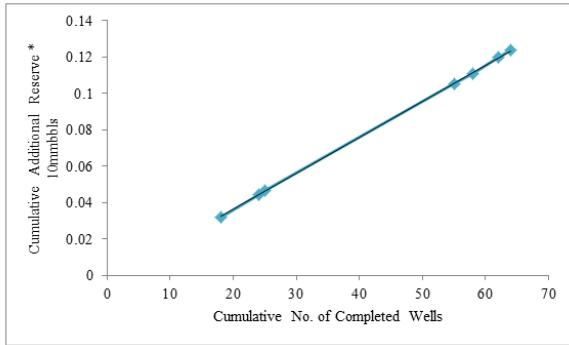


Figure 1: Cumulative Additional Reserves vs. Cumulative No. of Completed Wells for Field X.

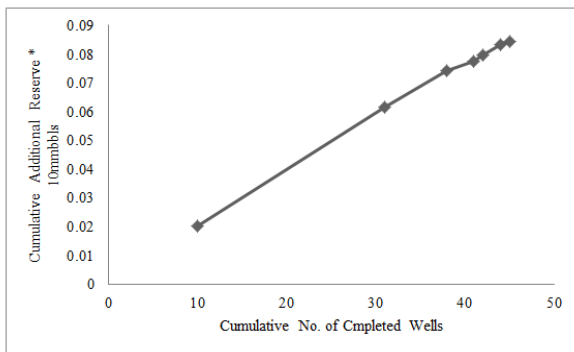


Figure 2: Cumulative Additional Reserves vs. Cumulative No. of Completed Wells for Field Y.

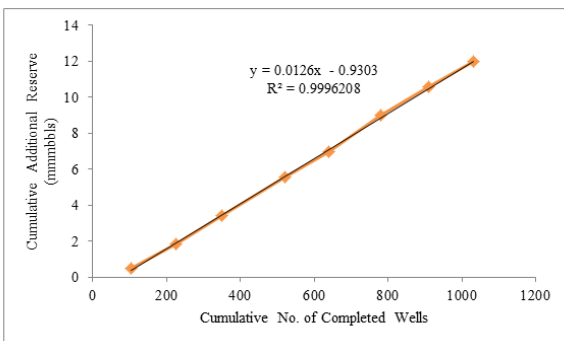


Figure 3: Cumulative Additional Reserves vs. Cumulative No. of Completed Wells for Nigeria.

DISCUSSION OF RESULTS

The cumulative additional reserve with cumulative number of completed wells varies from one field to the other and it is a function of hydrocarbon

potential of each field. A field with high hydrocarbon potential has a high rate of change of cumulative number of completed wells. For example the rate of change of cumulative additional reserves with cumulative number of completed wells of Field Y is larger than that of Field X. It shows that Field Y has a huge crude oil potential than Field X. Therefore the developed Estimation Model could be used as a benchmark to measure the hydrocarbon potential of a given field.

The variation between the estimated reserve and the actual reserve could be attributed to the assumption made in the application of the estimation model that no revision of the field samples has been used which makes the additional reserve due to the revision of the field to be zero. The additional reserve when added by way of revision could alter the reserve potential when increased knowledge of the field changes the field fractional recovery.

CONCLUSIONS

The following conclusions could be drawn from the findings:

- The Estimation model is useful in that better and more reliable reserve estimates are evaluated since the most recent data are used.
- The model gives an improved performance when compared between cumulative additional reserve and cumulative number of completed wells.
- The model depends on sound, accurate and up to date production data. Direct estimation of reserves in future will not be possible without first estimating the production during the year and reserve at the end of the preceding year.
- Reserves estimates of some existing fields could be considerably improved upon if such fields are revised by way of re-evaluating their basic geology and engineering data.

RECOMMENDATIONS

- The model only investigated the reserves in existing wells. Effort should be geared

towards evaluating reserves of unexpected fields.

- A mathematical expression that would relate the rate of change of cumulative additional reserve to cumulative number of completed wells be developed and incorporated into the model to replace the one evaluated from linear regression analysis.

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SUGGESTED CITATION

Oseh, J.O., I.A. Oguaman, and C.U. Omohimoria. 2014. "Alternate Method of Estimating Nigerian Hydrocarbon Reserves". *Pacific Journal of Science and Technology*. 16(1):50-59.

 [Pacific Journal of Science and Technology](http://www.akamaiuniversity.us/PJST.htm)